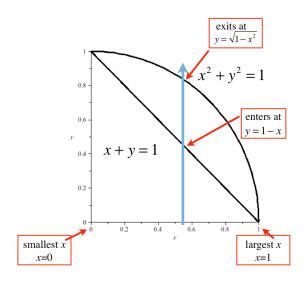
#### Math 213 - 11.3 Limits on Double Integrals

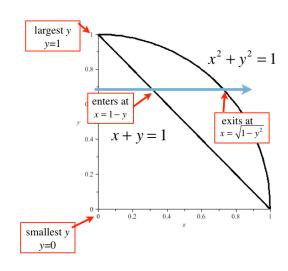
Suppose we wanted to find  $\int \int f(x,y)dA$  over the region bounded by the curves  $\begin{cases} x+y=1\\ x^2+y^2=1 \end{cases}$ .

## Suppose we wanted to integrate first with respect to y and then with respect to x.



$$\int_{x=0}^{x=1} \int_{y=1-x}^{y=\sqrt{1-x^2}} f(x,y) dy dx$$

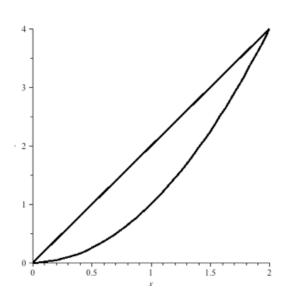
# Suppose we wanted to integrate first with respect to x and then with respect to y.



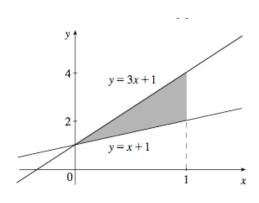
$$\int_{y=0}^{y=1} \int_{x=1-y}^{y=\sqrt{1-y^2}} f(x,y) dx dy$$

#### **Order Matters!**

### **Compute** $\int \int (4x+2)dA$

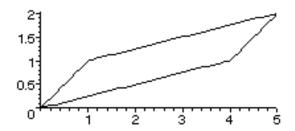


Compute 
$$\iint e^{x^2} dA$$



Fill in the required limit of integration for each of the following double integrals  $\iint_R f(x,y)dA$ , where R is the region indicated in the accompanying sketch.

1. 
$$\int_0^1 \int_{[?]}^{4y} f(x,y) dx dy + \int_1^2 \int_{[?]}^{[?]} f(x,y) dx dy$$



2. 
$$\int_0^3 \int_{[?]}^{[?]} f(x,y) dy dx + \int_3^5 \int_{[?]}^{[?]} f(x,y) dy dx$$

