

1. Suppose a function is given by a table of values as follows:

$x$	1.1	1.3	1.5	1.7	1.9	2.1
$f(x)$	12	15	21	23	24	25

- (a) Estimate the instantaneous rate of change of  $f$  at  $x = 1.7$ .
- (b) Use your answer in (a) to predict a value for  $f$  at  $x = 1.8$ .
- (c) Is your prediction too large or too small? Explain.
2. Let  $f(T)$  be the time, in minutes, that it takes for an oven to heat up to temperature  $T$  °F.
- (a) Give the meaning, in plain English, of  $f(300) = 10$ .
- (b) What are the units of  $f'(T)$ ?
- (c) Do you think  $f'(T)$  would be positive or negative?
- (d) Give the meaning, in plain English, of  $f'(300) = 0.1$
3. A sports car accelerates from 0 ft/sec to 88 ft/sec in 5 seconds (88 ft/sec = 60 mph) The car's velocity is given in the table below.

$t$	0	1	2	3	4	5
$V(t)$	0	30	52	68	80	88

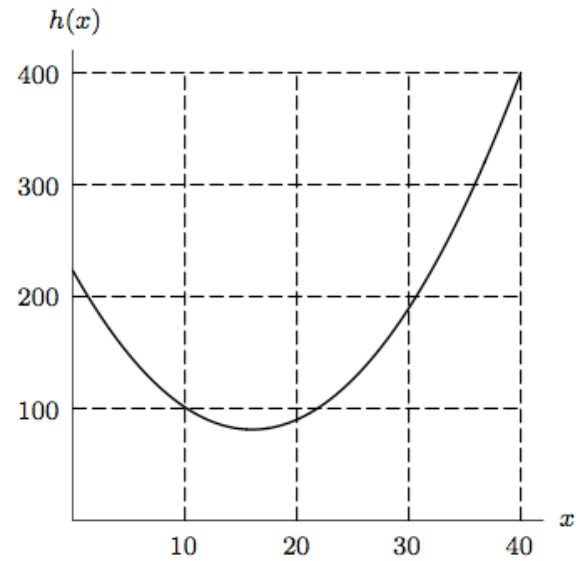
Find upper and lower bounds for the distance the car travels in 5 seconds.

4. Let  $f(t) = t^3 + t$ .
- (a) What is the total change in  $f(t)$  between  $t = 2$  and  $t = 5$ ?
- (b) What is the *average rate of change* in  $f(t)$  between  $t = 2$  and  $t = 5$ ?
5. The flow rate of water in a mountain stream due to spring runoff is given in the following table. Give your *best* estimate for the total volume of water from 6:00 pm to midnight.

time (hours since 6:00 pm)	0	1	2	3	4	5	6
flow rate (in cubic meters per hour)	300	360	410	455	490	520	545

6. The graph of  $h(x)$  is given to the right.

- (a) Draw on the graph (label your drawings and use different colors if you can)
  - (i) A line segment whose length equals the change  $\Delta h$  in  $h(x)$  between  $x = 20$  and  $x = 40$ .
  - (ii) A line segment whose slope equals the average rate of change  $\frac{\Delta h}{\Delta x}$  of  $h(x)$  between  $x = 20$  and  $x = 40$ .
  - (iii) A line whose slope equals the derivative  $h'(10)$ .
  - (iv) A point on the graph where  $h' = 0$ .

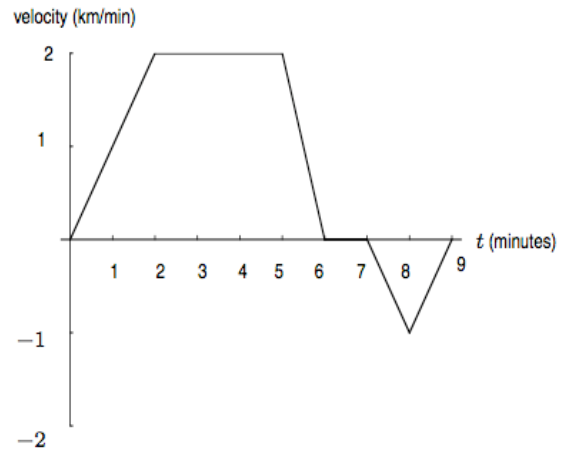


(b) Carefully estimate  $h(30)$

7. A car is moving along a straight road from A to B starting from A at time  $t = 0$ .



To the right is the velocity (in km/min) plotted against time (in min).



How many kilometers away from A is the car at time

- (b)  $t = 2$
- (c)  $t = 5$
- (d)  $t = 6$
- (e)  $t = 7$
- (f)  $t = 9$

8. Find the derivatives of the following functions. Do not simplify.

(a)  $f(x) = \sqrt{x}$

(e)  $y = \ln(x^3 + 4)$

(b)  $y = r^2 + 7r - 17$

(f)  $h(z) = z \cos(3z)$

(c)  $h(t) = t^2 + \sqrt{2}t$

(g)  $f(x) = \frac{\ln x + 5}{x^2 + 7}$

(d)  $g(x) = 2e^{\pi x}$

9. The temperature,  $Y$ , in degrees Fahrenheit of a yam in a hot oven  $t$  minutes after it is placed there is given by

$$Y(t) = 350(1 - 0.7e^{-0.008t})$$

(b) What was the temperature of the yam when it was placed in the oven?

(c) If the yam is left on in the oven for a long time, it will eventually reach the temperature of the oven. What is the temperature of the oven?

(d) When does the yam reach  $175^\circ \text{F}$ ?

(e) What is  $Y(20)$ ? What is  $Y'(20)$ ? What do these quantities tell us about the temperature of the yam?